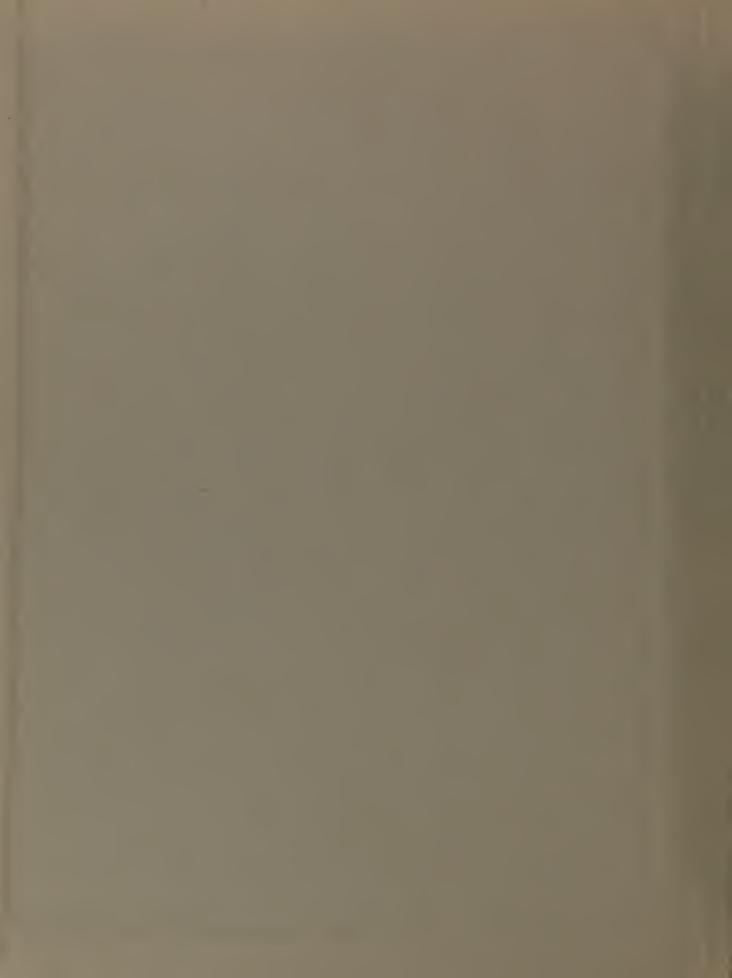
OPERATING CHARACTERISTICS OF A URANIUM GRAPHITE SUBCRITICAL ASSEMBLY WITH COOLANT SIMULATION John Henry Hoganson



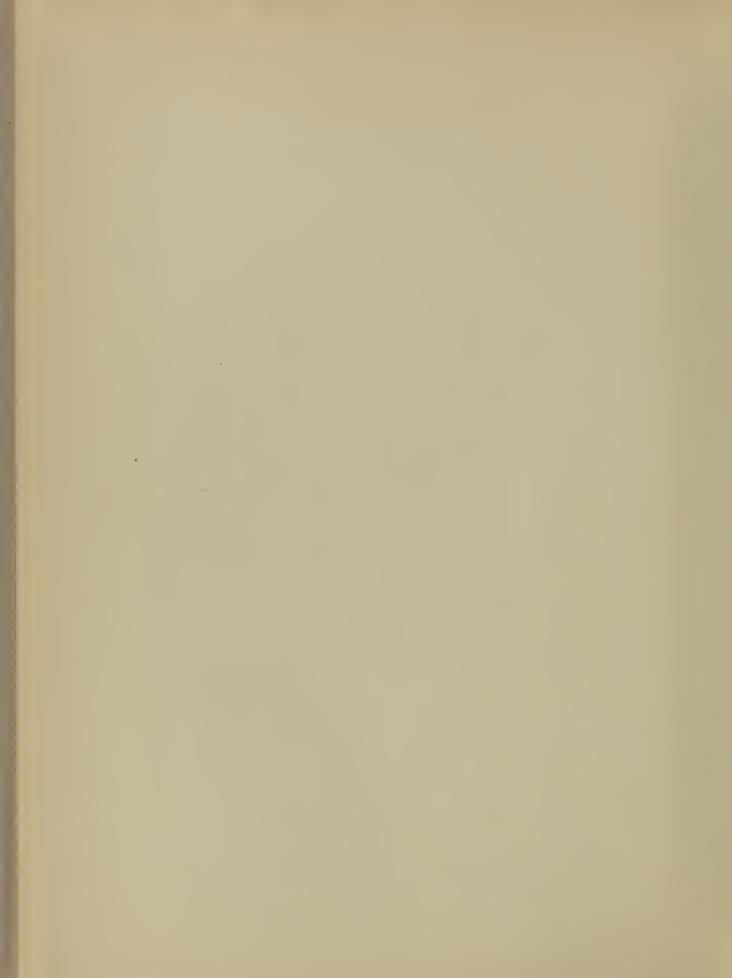


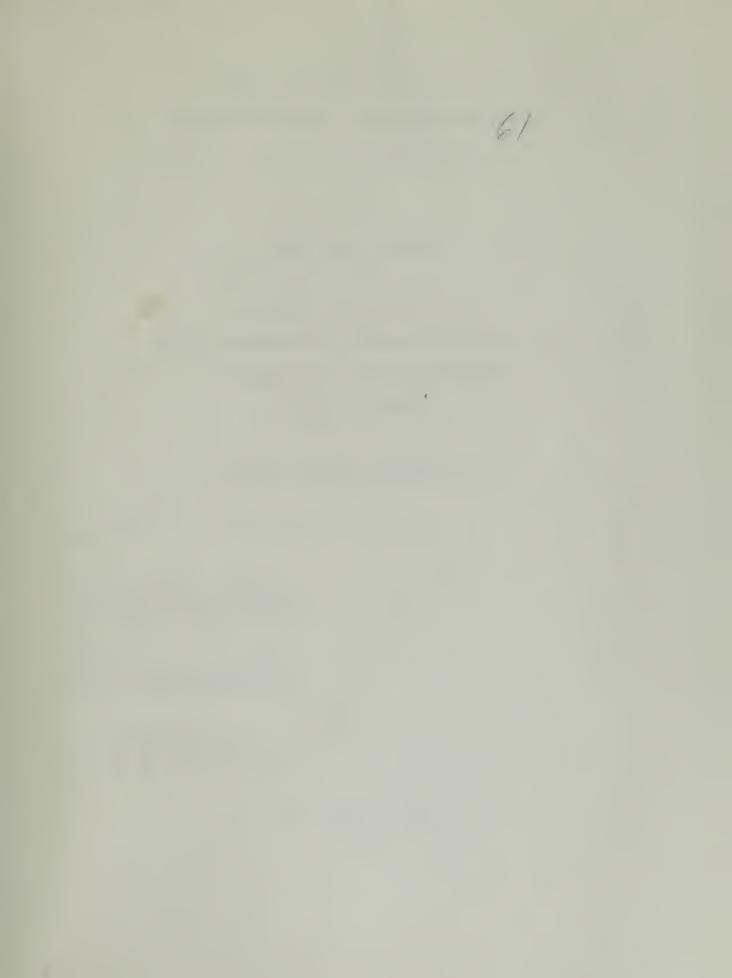


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OPERATING CHARACTERISTICS OF A URANIUM GRAPHITE SUBCRITICAL ASSEMBLY WITH COOLANT SIMULATION

by

John Henry Hoganson

A Thesis Submitted to the

Graduate Faculty in Fartial Fulfillment of

The Requirements for the Degree of

MASTER OF SCIENCE

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I. INTRODUCTION

The maximum power level of a nuclear reactor is frequently limited by the rate of heat removal. The actual design of a power reactor represents a compromise between the requirements of heat transfer and those of nuclear physics.

Nuclear reactor theory is not sufficiently accurate to guarantee that a particular reactor (especially one of a new design) will go critical. Therefore, the nuclear characteristics of a reactor design must be obtained before construction of the full scale reactor. Some of this information can be obtained from the use of a subcritical assembly.

Experiments with uranium graphite subcritical assemblies can be carried out to determine the various nuclear constants of a proposed reactor lattice. These lattice constants are the material buckling, multiplication constant, lattice diffusion length, and thermal utilization of the unit cell including the process tube assembly.

In this investigation six lattice configurations were considered, and the buckling of each was determined experimentally. Lattice cells of 6 in., 8.5 in., and 12 in., denoted I, II, and III respectively, constituted the three geometric lattice arrangements. For each of these, both the "wet" and "dry" cases were considered. The measurements and calculations with water present in the cooling annulus were

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designated as "wet", and those with the process tube, but without water, as "dry".

These six lattice configurations were also considered in the theoretical analysis. The buckling of each of the six lattice configurations was determined theoretically by two methods. Only one size fuel element and one size process tubing was used in the experimental and theoretical analyses of this investigation.

The methods of Murray (1) and of Rumsey and Volkoff (2), (3) were used to determine theoretically the thermal utilization and the resonance escape probability. Murray's method was shown to give less conservative results than the method of Fumsey and Volkoff. The theoretical multiplication constant derived for each configuration considered was based on literature and calculated values of the various diffusion lengths, the Fermi age, and the various macroscopic cross sections. The product of 7 and \in was assumed to be essentially constant for the various configurations investigated.

Analyses of the data for the given configurations were carried out by use of the classical formula for the buckling

$$B^{2} = \frac{\eta \in \text{pf} - 1}{L^{2} + \eta \in \text{pf} \gamma}$$
 (1)

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A comparison between the "wet" and "dry" cases of the three lattice cells considered was presented using the experimental and theoretical values of the buckling. By an analysis of the results obtained in this investigation, the effect of the water coolant on the nuclear properties of the various lattice configurations was determined.

II. REVIEW OF LITERATURE

The theoretical calculation of the multiplication factor for a heterogeneous reactor with coolant is an extension to the method of calculating the thermal utilization and resonance escape probability factors for an infinite heterogeneous uranium-graphite reactor presented by Weinberg (4), (5).

Guggenheim and Pryce (6) extended the method to include a non-absorbing coolant and a thin sheath of absorbant aluminum around the fuel element. Houston (7) extended the method to include neutron absorption in a coolant. Houston's results are more suitable for gas or heavy liquid metal cooled reactors due to his assumptions concerning the coolant's negligible moderating properties and small volume fraction of the lattice cell. Rumsey and Volkoff (2), (3) extended the above methods further to include the moderating effect of a water annulus.

Murray (1) presented a simplified method of calculating the thermal utilization which considers all but the uranium and the graphite in the lattice cell as poisons which reduce the basic uranium graphite thermal utilization. Murray's method for the calculation of the resonance escape probability does not consider the so called poisons. The Rumsey and Volkoff method appears to be at the present time the most comprehensive theoretical analysis of a water cooled uranium-graphite lattice cell.

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The experiments with subcritical assemblies of the Hanford Atomic Products Operation included an effort to determine the effect of a water annulus around the fuel element on the buckling. The effect of aluminum, air, and other impurities in the lattice upon the buckling was also investigated (8). A few measurements were taken using internally cooled cylindrical fuel rods, but the majority of the coolant simulation experiments were with solid cylindrical fuel rods of natural uranium surrounded by an annulus of water. The objectives of the subcritical assembly experiments at Hanford (3) were to determine experimentally the various lattice constants. The existing lattice theory was supplemented and improved where possible. Lattice measurements were taken with three different fuel rod diameters: 0.925 in., 1.175 in., and 1.36 in. The lattice spacing and the water-aluminum-uranium ratios were varied for each slug size.

The results of the series of tests using both "wet" and "dry" lattices were compiled by Clayton (9). A comparison of theory and experimental results for one fuel element diameter, six lattice spacings, and the "wet" and "dry" configurations for the Hanford Atomic Products Operation was done by Gast and others (2). Gast used the method of Rumsey and Volkoff to calculate the theoretical values of the thermal utilization and the resonance escape probability.

Related conclusions (8) from the Hanford work with water cooled uranium graphite lattices were:

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- (a) For a given natural uranium fuel assembly, there is a maximum in the buckling vs. C/U atom ratio curve. The slug diameter and the water annulus thickness are inversely proportional to the value of C/U at which the maximum occurs. This maximum occurs between C/U values of 50 and 100.
- (b) The buckling "dry" is greater than the buckling "wet" for larger lattice spacings (C/U atom ratio). As the lattice spacing is decreased, the buckling curves cross and the "wet" buckling becomes greater than the "dry" buckling. For this lower C/U atom ratio region, externally cooled slugs exhibit a "fail-safe" behavior on the loss of water.

The following conclusions were a result of the Hanford experiments(2). The state of the heterogeneous graphite uranium lattice theory at present is not completely satisfactory. More experimental measurements of individual parameters such as f and p are necessary in order to establish the basis for an improved theoretical analysis. Corrections for variations in reactor material densities and purities, and allowances for holes, such as for control rods, need further investigation (2). Finally, the treatment of the energy spectrum of neutrons, fast to thermal, requires more accurate development of neutron resonance and capture reactions.

III. THEORETICAL ANALYSIS

A. General Procedure

The product of the fast fission factor, \in , the primary fission neutron factor, η , the thermal utilization factor, f, and the resonance escape factor, f, is the infinite multiplication constant, f, f.

$$\epsilon \gamma \Gamma p = k_{\infty}$$
(2)

A theoretical analysis of each of the factors would have been extremely complicated without certain simplifying assumptions. These assumptions are stated where applicable in the following theory. Each of the factors was considered separately. The product En was determined and assumed constant for all the lattice configurations considered. Expressions for f and p were determined using the methods of Murray, denoted Method A, and the methods of Rumsey and Volkoff, denoted Method B, for the "wet" and "dry" cases of Lattices I, II and III.

Using values from the literature for the lattice diffusion length and the Fermi age with the theoretically determined infinite multiplication constant, the buckling was determined from Equation 1. The theoretical buckling was determined

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for Lattices I, II, and III for both the "wet" and "dry" cases using both Methods A and B.

The effect of the air annulus and air holes on the neutron density in all lattice geometries was neglected due to the magnitude of the effect in comparison with other material effects in the lattice.

Subscripts used in this analysis were defined as follows:

- u natural uranium
- al slug can, 25 aluminum
- w water
- g graphite
- m moderator
- p process tube, 61S aluminum
- a absorption
- s scattering
- re resonance
- sa scattering "absorption"
- f slow neutron fission
- t transport theory

Any deviation of notation from the above list was individually defined.

B. Fast Pission Factor

The fast fission factor, €, is the ratio of the total number of neutrons produced by fission to the number of neutrons

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produced by fission by thermal neutrons. Assuming that the primary neutron source is distributed approximately uniformly over the fuel, a simplified version of the equation given by Glasstone and Edlund (5, p. 278) for the fast fission factor is

$$\epsilon - 1 = \frac{\left[(y - 1) - \frac{\sigma_c}{\sigma_f} \right] \frac{\sigma_f}{\sigma_t} P}{1 - P \left(\frac{y \sigma_f + \sigma_e}{\sigma_t} \right)} = \frac{(\eta - 1) \frac{\sigma_a}{\sigma_t} P}{1 - \frac{P}{\sigma_t} (\eta \sigma_a + \sigma_e)}$$
 (3)

- where P is the probability that a fission neutron born in a rod will make a collision inside the rod in which it was created;
 - Ta is the absorption cross section for fast neutrons, that is, the sum of the fission and the capture cross sections:
 - Ta is the elastic cross section for fast neutrons;
 - σ, is the inelastic cross section for fast neutrons;
- and σ_t is the total cross section for fast neutrons.

$$\sigma_t = \sigma_a + \sigma_e + \sigma_i$$
.

Using fast neutron cross section values as given by Guggenheim and Pryce (6, p. 51), Equation 3 reduces to

$$\epsilon - 1 = \frac{0.0948 \text{ P}}{1 - 0.521 \text{ P}} \tag{4}$$

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These numerical coefficients are such that when the fuel element radius is less than 1.7 cm the calculated value of ϵ agrees reasonably well with experimental results obtained by Argonne National Laboratory (6, p.51). For natural uranium of density 19 g/cm³ and a rod radius of 0.5 in., the value of N $\sigma_{\rm t}$ ru is 0.262, where N is the number of uranium atoms per unit volume, and ru is the radius of the fuel rod. The quantity P is a function of N $\sigma_{\rm t}$ ru. From a relationship of P and N $\sigma_{\rm t}$ ru shown by Guggenheim and Pryce (6, p. 51) and the above computed value of N $\sigma_{\rm t}$ ru, the value of P determined was 0.25.

Solving Equation 4 for & gave a value of 1.027. This value for the fast fission factor was assumed constant for all configurations investigated.

C. Primary Pission Neutrons

The number of fission neutrons released per thermal neutron captured in the fuel is the factor, η . Glasstone and Edlund define η (5, p. 83) as

$$\eta = \frac{\nu \sum_{f}^{u}}{\sum_{a}^{u}}$$
 (5)

where " is the average number of neutrons produced per thermal neutron fission;

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and \sum_{a}^{a} is the total cross section for absorption of thermal neutrons.

The microscopic thermal fission cross section for natural uranium is 4.18 barns. Applying the maxwellian distribution correction of 1.128 and the "not - 1/v" factor of 0.981 for U²³⁵ to this value gives an effective fission cross section of 3.635 barns for natural uranium. The microscopic thermal absorption cross section for natural uranium is 7.68 barns. Applying the maxwellian distribution correction and a "not - 1/v" factor of 0.990 for natural uranium to this value determines an effective absorption cross section of 6.74 barns for natural uranium (1, p. 32).

Murray (1, p. 98) gives a value of 2.46 for ν . Substituting the above quantities in Equation 5, the calculated value of η was 1.327.

It is normal practice in working with subcritical assemblies to experimentally determine k_{∞} and then divide k_{∞} by the product ϵ pf to arrive at a value of η . The value of η found by subcritical assembly experiments was 1.308 neutrons per thermal neutron captured (10, p. 85). This value is in reasonable agreement to the computed value of 1.327. The value of η used in the following analysis was 1.308 and was assumed constant for all configurations investigated.

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D. Thormal Utilization

In heterogeneous lattice theory the finite lattice reactor is assumed to be an infinite lattice array. The problem of calculating f and p is simplified by replacing the
square cells by equivalent cylindrical unit cells. Table 1
gives the equivalent cell dimensions for Lattices I, II, and
III. Assuming that little change in the overall neutron
flux is experienced in traversing one cell, an individual
cell may be representative of the total.

The methods of Murray (1) and of Rumsey and Volkoff (2), (3) were used to determine theoretically the thermal utilization. These methods were considered separately and were denoted Methods A and B respectively.

1. Method A

The depression of the thermal neutron flux in the fuel and adjacent moderator complicates the calculation of the thermal utilization. Average flux and volume weighting factors must both be included in the fractional absorption of the fuel. From the spatial variation of the flux in a cell, the average values of the flux can be determined.

The thermal neutron diffusion equations for the uranium and the moderator from diffusion theory are

$$D_{u} \nabla^{2} \not S_{u} - \not S_{u} \Sigma_{u} + S_{u} = 0 \tag{6}$$

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(4)

and

$$D_m \nabla^2 \beta_m - \beta_m \sum_m + S_m = 0 \tag{7}$$

Equations 6 and 7 can be simplified with the following assumptions:

- (a) The variation of neutron flux at a given cell radius will be the same everywhere.
- (b) There are no thermal neutrons produced in the uranium. S, is zero.
- (c) The production rate of thermal neutrons in the moderator is independent of position. S_m is constant.
- (d) The flux is assumed not to vary along the fuel cell axis.

Using the above assumptions and cylindrical coordinates, Equation 6 for the fuel becomes

$$\frac{\mathrm{d}^2 \beta_{\mathrm{u}}}{\mathrm{d} x^2} + \frac{1}{x} \left(\frac{\mathrm{d} \beta_{\mathrm{u}}}{\mathrm{d} x} \right) - \beta_{\mathrm{u}} = 0 \tag{8}$$

where $x = \mathcal{H}_{u}^{r}$ and \mathcal{H}_{u}^{r} is the inverse diffusion length of uranium, and Equation 7 for the moderator becomes

$$\frac{\mathrm{d}^2 \not p_m}{\mathrm{d}r^2} + \frac{1}{r} \left(\frac{\mathrm{d} \not p_m}{\mathrm{d}r} \right) - \partial \not p_m^2 \not p_m = -\frac{s_m}{D_m} \tag{9}$$

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where P_m is the diffusion coefficient for the moderator. R^2 is the square of the inverse diffusion length.

Equation 8 for the fuel is the modified Bessel equation of zero order. Equation 9 for the moderator is the inhomogeneous type of the modified Bessel equation of zero order. The solutions of Equations 8 and 9 are

$$\beta_{ij}(\mathbf{r}) = \mathbf{A} \mathbf{I}_{0} \left(\mathbf{H}_{ij} \mathbf{r} \right) \tag{10}$$

and
$$\beta_{m}(r) = C K_{0} (H_{m}r) + G I_{0} (H_{m}r) + \frac{S_{m}}{\Sigma_{m}}$$
 (11)

respectively. The boundary conditions used in the evaluation of the constants A, C, and G are neutron flux and current continuity at $r = r_u$ (uranium rod radius) and the condition that $d\phi_m/dr = 0$ at $r = r_2$ (the equivalent outer radius of the graphite cell).

Applying the condition of zero neutron current at r_2 in Equation 11

$$G = C \frac{K_1 (H_m r_2)}{I_1 (H_m r_2)}$$
 (12)

thus the moderator flux, Equation 11, becomes

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where

$$M_0 \left(\mathcal{H}_m \mathbf{r} \right) = K_0 \left(\mathcal{H}_m \mathbf{r} \right) + \frac{K_1 \left(\mathcal{H}_m \mathbf{r}_2 \right)}{I_1 \left(\mathcal{H}_m \mathbf{r}_2 \right)} I_0 \left(\mathcal{H}_m \mathbf{r} \right)$$

Continuity of flux and current at r_u gives a pair of equations from Equations 10 and 13 which can be solved simultaneously to give

$$\frac{A}{S_m} = \frac{D_m \mathcal{H}_m \mathcal{H}_1 (\mathcal{H}_m r_u)}{\Delta} \tag{14}$$

and
$$\frac{C}{S_m} = -\frac{D_u H_u I_1 (H_u r_u)}{\Delta}$$
 (15)

where
$$M_1 (\mathcal{H}_m r) = K_1 (\mathcal{H}_m r) - \frac{K_1 (\mathcal{H}_m r_2)}{I_1 (\mathcal{H}_m r_2)} I_1 (\mathcal{H}_m r)$$

and
$$\Delta = \sum_{m} \left[D_{m} \mathcal{H}_{m} I_{0} (\mathcal{H}_{u} r_{u}) M_{1} (\mathcal{H}_{m} r_{u}) + D_{u} \mathcal{H}_{u} I_{1} (\mathcal{H}_{u} r_{u}) M_{0} (\mathcal{H}_{m} r_{u}) \right]$$

with $\frac{dN_0(x)}{dx} = -M_1(x) .$

The thermal utilization, f, is the ratio of the thermal neutrons absorbed in the fuel to the total thermal neutrons absorbed. This ratio is equivalent to the ratio of the thermal neutron mal neutrons absorbed in the fuel to the total thermal neutron source assuming no net leakage from the cell.

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$$f = \frac{\int_{0}^{r_{u}} \beta_{u} \sum_{u} 2\pi r dr}{V_{m} S_{m}}$$
 (16)

Combining Equation 10 and 16 into

$$f = \left(\frac{A}{S_m}\right) \frac{2\pi}{V_m} \int_0^{\mathbf{r}_u} I_0 \left(\mathbf{P}_u\mathbf{r}\right) \mathbf{r} d\mathbf{r}$$
 (17)

and solving the integral (1, p. 305) gives

$$f = \left(\frac{A}{S_m}\right) \frac{2\pi \sum_{u} \frac{\sum_{u} r_u I_1 (H_u r_u)}{H_u}$$
 (18)

Combining Equations 14 and 18 and solving for the reciprocal of f gives

$$\frac{1}{f} = 1 + \frac{V_m \frac{\Sigma}{m}}{V_u \frac{\Sigma}{\Sigma}} F + (E - 1)$$
 (19)

where

$$F = \frac{\mathcal{H}_{u}r_{u}}{2} \frac{I_{0} \left(\mathcal{H}_{u}r_{u}\right)}{I_{1} \left(\mathcal{H}_{u}r_{u}\right)}$$
(20)

and
$$E - 1 = \begin{bmatrix} V_{m} & \mathcal{F}_{m} r_{u} & \frac{M_{0} (\mathcal{F}_{m} r_{u})}{2} \\ V_{u} & 2 & \frac{M_{1} (\mathcal{F}_{m} r_{u})}{2} \end{bmatrix} - 1$$
(21)

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F is the disadvantage factor of the uranium which is the ratio of the neutron flux at the rod surface to the average flux in the rod interior (5, p.270).

$$F = \frac{\beta_{u}(\mathbf{r}_{u})}{\overline{\beta}_{u}} \tag{22}$$

The average thermal neutron flux in the moderator is greater than the thermal neutron flux at the rod surface because the diffusion coefficient in the moderator is finite. The additional absorption is measured by the quantity (E-1), the excess absorption term.

Murray (1, p. 100) assumed that any poisons that are tolerable do not appreciably disturb the basic neutron flux distribution from that of the configuration with fuel and moderator only. Therefore, the aluminum cladding, coolant, and the process tube assembly can all be treated as poisons. The reciprocal thermal utilization with this modification can be written

$$\frac{1}{\ell_{p}} = \frac{1}{\ell} + \sum_{i=0}^{n \text{ poisons}} \frac{V_{1} \Sigma_{1} \overline{\beta}_{1}}{V_{u} \Sigma_{u} \overline{\beta}_{u}}$$
 (23)

where the average neutron flux in the added poison or absorber is \overline{p}_i .

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ess tube the ratio β_1/β_0 is approximately equal to β_1/β_0 , Equation 23 can be solved directly. Murray (1, p. 100) suggested that a slight refinement to Equation 23 may be made by letting Σ_1 be the difference between the actual poison cross section and the moderator cross section that it physically replaces.

Littler and Raffle (10, p. 94) give a useful approximation for the excess absorption term, E - 1.

$$E - 1 = \frac{r_2^2 r_2^2}{2} \left[\frac{r_2^2}{r_2^2 - r_1^2} \ln \frac{r_2}{r_1} - \frac{3}{4} + \frac{r_1^2}{4r_2^2} \right]$$
 (24)

The constants used in Equation 23 were listed in Tables 1 and 2. The equivalent cell dimensions were derived from direct measurements and calculations. The thermal neutron macroscopic cross sections for aluminum (cladding), water, and graphite were calculated from Equation 25 using literature values of σ_{α} (1), (5), and (11).

$$\Sigma = \frac{e \sigma^{N_0}}{A} \tag{25}$$

where N_0 is 6.02 x 10^{23} nuclei/mole, and A is the mass number.

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 $\Sigma_{\rm a}^{\rm p}$ for the aluminum process tube was calculated using a modification of Equation 25 to account for the alloying materials in the aluminum alloy. The maxwellian distribution correction and a "not-1/v" correction was used to determine an effective absorption cross section for natural uranium. All the macroscopic cross section values used in this theoretical analysis are shown in Table 2.

Due to the limitations of simple diffusion theory, transport theory must be used for the calculation of \mathcal{H}_u . Murray (1, p. 88) gives for the uranium fuel the relationship

$$\frac{\mathcal{H}_{u}}{\Sigma^{u}} = \tanh \frac{\mathcal{H}_{u}}{\Sigma^{u}_{s}}$$
 (26)

where \sum^{u} is the total cross section.

Solving Equation 25 using cross section values from Table 2 gave a value of 0.675 cm⁻¹ for \mathcal{H}_{u} . The inverse diffusion lengths for graphite and water were found using Equation 27 and values of the diffusion lengths from the literature (5).

$$\mathcal{H} = \frac{1}{L} = \left(\sum_{\mathbf{a}} / \mathbf{D} \right)^{1/2} \tag{27}$$

The thermal utilizations for the dry lattice configurations were calculated by omitting the term for water in Equation 23. The volume ratios in Equation 19 and 23 are equivalent to area ratios.

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The constants listed in Tables 1 and 2 were used in Equations 19, 20, 23, and 24 to evaluate the composite thermal utilizations for the various lattice configurations considered. A Bessel function table (12) was used to evaluate the disadvantage factor, F, in Equation 20. Equation 24 was used to evaluate the excess absorption torm, (E - 1).

The resulting thermal utilizations computed by Method A are listed in Table 3 for the various lattice configurations.

2. Method B

A second method of calculating the thermal utilization of uranium is the method of Rumsey and Volkoff (2), (3). This method is an extension of prior work in heterogeneous lattice theory (4), (6) and includes the moderating effect of a water annulus in the lattice cell.

$$f_u = f_0 (1 + 6)$$
 (28)

where
$$\frac{1}{f_0} - 1 = R_{al} + R_p + R_w + R_g + S_w + S_g + B_{wp} + B_{wg}$$
 (29)

and
$$\delta = \frac{q_W V_W}{q_g V_g} \left[(E - 1) + \frac{1}{2} H^2 t_W^2 t_W^2 \frac{N_g \sigma_g V_g}{N_W \sigma_W V_W} \right]$$

$$1 + \frac{q_W V_W}{q_g V_g}$$
(30)

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The "relative absorption" term, R_j, denotes per thermal neutron captured in the uranium, the number of thermal neutrons which would be captured in the jth medium if the neutron density in the jth medium were uniformly equal to the neutron density at the uranium-aluminum interface.

$$R_{j} = \frac{N_{j} \sigma_{j} V_{j}}{N_{u} \sigma_{u} V_{u}} F = \frac{\sum_{j} V_{j}}{\sum_{u} V_{u}} \cdot F$$
 (31)

where F is the disadvantage factor of the uranium, Equation 20.

The "self blocking" term, S_j , denotes per thermal neutron absorbed in the uranium, the excess number of thermal neutrons captured in the jth medium due to the excess density of neutrons in the jth medium over the neutron density at the i-jth interface.

$$S_{W} = \frac{1}{2} H_{W}^{2} t_{W}^{2}$$
 (32)

and
$$S_g = (E - 1) \left[1 + R_{al} + R_p + R_w + B_{wp} + S_w \right]$$
 (33)

where (E - 1) is the disadvantage factor of the moderator or excess absorption term given by Equation 24.

The "blocking term", Bij, denotes per thermal neutron absorbed in uranium, the excess number of thermal neutrons

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captured in the jth medium due to neutron density rise across the ith medium.

$$B_{WP} = \mathcal{H}_{W}^{2} t_{W}^{2} \frac{N_{P} \sigma_{P} V_{P}}{N_{W} \sigma_{W} V_{W}} = \mathcal{H}_{W}^{2} t_{W}^{2} \frac{\Sigma_{P} V_{P}}{\Sigma_{W} V_{W}}$$
(34)

and
$$B_{Wg} = H_W^2 t_W^2 \left\{ \frac{N_g \sigma_g V_g}{N_W \sigma_W V_W} + R_g \left[\frac{1}{2} + \frac{N_{al} \sigma_{al} (V_{cap} + can)}{N_W \sigma_W V_W} \right] \right\}$$
(35)

In the above six equations \mathcal{H}_W is the inverse diffusion length of water, and \mathbf{t}_W is the thickness of the water annulus. The cross section values are listed in Table 2, and the volume values per slug are listed in Table 1. The value of (-1) is given by Equation 2h which is an approximation of the complex Bessel function in Equation 21. The approximation is considered to be sufficiently accurate for the two lattice geometries.

The production rate of thermal neutrons per unit volume per second for water and graphite are denoted q_w and q_g respectively. The ratio of the slowing down power of water to graphite, q_w/q_g , equals 20 (3, p. 22).

Figure 1 and Figure 2 show the neutron density distribution in the dry and wet lattice configurations respectively. The several terms of the competitive absorption, Equation 29, are shown schematically in these diagrams. The placement of The same of the sa

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the individual absorption terms, defined in Equations 31 through 35, and the relative magnitude of these various terms can also be seen in the diagram. Any absorption of neutrons by the air in the air annulus was neglected. The net flow of thermal neutrons across the boundary of a cell was assumed to be zero.

The terms S_{al}, S_p, B_{alw}, B_{alp}, B_{alg}, and B_{pg} which are shown in Figure 1 and Figure 2 were assumed as negligible and were not included in Equation 29. At the uranium-aluminum interface, continuity of the neutron flux density and current density was assumed. The neutron current density was also assumed as linear through the thin mediums (al, p, or w) considered.

As an example, in deriving the Sal term, the aluminum surface neutron flux is

$$\beta_{al}$$
 surface = $\beta_{u}(r_{u}) + t_{al} \left(\frac{d\beta_{al}}{dr}\right)_{r_{u}}$

and with Equation (10) is

$$\beta_{al}$$
 surface = $\beta_{u}(r_{u}) + t_{al}$ $\left(\frac{D_{u}}{D_{al}}\right)$ A $\beta_{u} I_{l} (\beta_{u} r_{u})$

By definition the "self blocking" term for aluminum is

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$$S_{al} = \frac{\left(\beta_{al}^{ave} - \beta_{u}^{surface}\right)}{\beta_{u}^{ave}} \frac{v_{al} \Sigma_{a}^{al}}{v_{u} \Sigma_{a}^{u}}$$
(36)

and taking from (10, p. 89)

$$\beta_{u}^{\text{ave}} = \frac{2A}{\mathcal{H}_{u}r_{u}} I_{1} (\mathcal{H}_{u}r_{u})$$

and substituting gives

$$s_{al} = \frac{1}{2} t_{al}^2 \theta_{al}^2 \tag{37}$$

Similarly

$$S_{W} \cong \frac{1}{2} t_{W}^{2} H_{W}^{2} \tag{32}$$

and

$$s_p = \frac{1}{2} t_p^2 H_p^2$$

A calculation of S_{al} , Equation 37, showed that with $H_{al}^2 = 0.002 \mu \mu \text{ cm}^{-2}$ (10, p. 93) and $t_{al} = 0.102 \text{ cm}$, that $S_{al} = 1.27 \times 10^{-5}$. This value is of a magnitude which can be considered negligible.

The very small factor, $(H_i t_i)^2$, for the cladding and process tube causes the terms S_{al} , S_p , B_{alw} , B_{alp} , B_{alp} , and B_p to become negligible with respect to the other terms in Figure 1 and Figure 2. With these eliminations, Figure 1 and Figure 2 agree with Equation 29.

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The constants listed in Tables 1 and 2 were used in Equations 28 through 35 to evaluate the wet configuration thermal utilizations by the Rumsey and Volkoff method. Equation 20 was used to evaluate F in Equation 31. The value (E-1) in Equation 33 was evaluated by using Equation 24. The thermal utilizations for the dry configurations were calculated using Equations 28 through 35 with the terms for water omitted. The resulting thermal utilizations, Method E, are listed in Table 3 for the various configurations.

E. Resonance Escape Probability

The fraction of fast fission neutrons that reach thermal energy without experiencing capture while slowing down, is called the resonance escape probability, p. The methods of Murray (1) and of Rumsey and Volkoff (2) were also used to theoretically determine the resonance escape factor. These methods are considered separately and are denoted Methods A and B respectively.

1. Method A

Murray (1, p. 92) gives the heterogeneous equivalent for p as

$$p = \exp \left[-\frac{v_u \, \bar{\beta}_u \, \sum_{re}^u}{v_m \, \bar{\beta}_m \, \xi \, \sum_{s}^m} \right]$$
 (38)

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where Σ_{re}^{u} is the effective macroscopic cross section. The form of Equation 38 suggests a resemblance to similar ratios appearing in the expression to evaluate f.

A definition of the resonance utilization, fr, is

The resonance absorption by the uranium is $\beta_u \vee_u \Sigma_0$ from a thermal flux absorption analogy, where Σ_0 is an appropriately chosen average cross section of uranium over the entire resonance flux region.

Assuming that the flux over the resonance region is 1/E dependent, the average cross section is

$$\bar{\sigma}_{u} = \frac{\int \sigma_{a}^{u} \frac{dE}{E}}{\int \frac{dE}{E}} = \frac{\sigma_{r}}{\ln \frac{E_{1}}{E_{2}}}$$
(40)

where $\ln \frac{E_1}{E_2} = 5.6$ for uranium metal (5, p. 273). The presence of the moderator and the geometric nature of the heterogeneous lattice requires that an effective resonance integral (σ_{re}) be used for the value of σ_r . Equation 40 is then

$$\overline{\sigma_{u}} = \frac{\sigma_{re}^{u}}{5.6} \tag{41}$$

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where (1, p. 93)

$$\sigma^{u} = \int (\sigma_{au}) \text{ off } \frac{dE}{L} = 9.25 + 24.7 \text{ S/M}$$
 (42)

and S/M is the fuel surface to mass ratio in cm2/g.

Finally
$$\Sigma_0 = \frac{N_u \sigma_{re}^u}{5.6} = \frac{\Sigma_{re}^u}{5.6}$$
 (43)

The scattering "absorption" by the moderator would be $\vec{p}_m \ v_m \ \sum_{i=1}^m from a thermal flux absorption analogy,$

where
$$\Sigma_{1}^{m} = \frac{f + \Sigma_{s}^{g} \frac{dE}{E}}{f \frac{dE}{E}} = \frac{f \Sigma_{s}^{g}}{5.6}$$
 (144)

With Equations 39, 43, and 44 the magnitude of the exponent of p in Equation 38 is

$$\frac{v_u \, \overline{\beta}_u \, \Sigma_{re}^u}{v_m \, \overline{\beta}_m \, | \, \Sigma_s^m} = \left(\frac{1}{r} - 1\right)^{-1} \tag{45}$$

Murray (1, p. 94) gives an empirical expression for the effective resonance inverse diffusion length of uranium,

$$H_{u}^{re} = 0.0222 \rho_{u} \text{ cm}^{-1}$$
 (46)

where ρ_{α} is expressed in g/cm^3 .

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The effective resonance inverse diffusion length for graphite is,

$$H_{E}^{re} = \sqrt{3 \sum_{1}^{m} \sum_{t}^{E}}$$
 (47)

where $\Sigma_{\mathbf{t}}^g$ is the actual transport cross section of the graphite averaged over the entire resonance flux region. To evaluate $\Sigma_{\mathbf{t}}^g$, the relationship

$$\sum_{t}^{g} = \sum_{s}^{g} (1 - \overline{\cos \theta})$$
 (48)

is derived from (5, p. 98)

$$\lambda_{\pm} = \lambda_{e}/1 - \cos \theta \tag{49}$$

where
$$\cos \theta = 2/3A$$
 (50)

and A is the moderator mass number.

The method of calculating f is now borrowed to find $f_{\mathbf{r}}$. Equation 19 modified is

$$\frac{1}{T_{\mathbf{r}}} = 1 + \frac{V_{\mathbf{g}}}{V_{\mathbf{u}}} \frac{\sum_{i=1}^{m}}{\sum_{i=1}^{m}} F + (E - 1)$$
 (51)

The values of u and u and u were determined from Equations 46 and 47. Σ_0 and Σ_1^m were calculated from Equations 43 and 44.

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Using the above values of K_u^{re} and K_g^{re} , F was determined from Equation 20 and (E - 1) was determined from Equation 24.

Table 2 lists all the important lattice material constants.

Solving Equation 51 and using the value of fr in Equation 45 determined the exponent of p in Equation 38. The resonance escape probabilities for the various configurations, Method A, are listed in Table 3. The values of p for the wet and dry configurations were the same using Method A.

2. Method B

Volkoff and Rumsey (2, p. 293) express the equation for the resonance escape probability as

$$p = \exp \left[-\frac{f_r}{1 - f_r} \right] \tag{52}$$

where f_p is the resonance utilization of uranium for resonance neutrons. Noting the form similarity of the exponent of Equation 52 to the thermal utilization equations, the factor, f_p , is

$$f_r = f_0 (1 + \delta) \tag{53}$$

with

$$\frac{1}{f_0} - 1 = R_{a1} + R_p + R_w + R_g + S_w + S_g + B_{wp} + B_{wg}$$
 (54)

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changing the cross sections Σ_a^u to Σ_0 and Σ_a^g to Σ_1^m in Equations 31, 33, and 35 gives a solution to Louation 54. δ is given by Equation 30.

Substituting the individual terms in Equation 54 gives

where
$$Z = \frac{F}{\Sigma_0 V_u} \left\{ \sum_{1}^{m} V_g \left[1 + \frac{F_u^2}{V_w} t_w^2 \left(\frac{1}{2} + \frac{\sum_{al} V_{eap} + can}{\sum_{w} V_w} \right) \right] + (E) \left(\sum_{al} V_{al} + \sum_{p} V_p + \sum_{w} V_w \right) \right\}$$
and
$$Y = \frac{F_w^2}{V_w^2} t_w^2 \left\{ \frac{1}{\sum_{w} V_w} \left[(E) \sum_{p} V_p + \sum_{l}^{m} V_g \right] + \frac{E}{2} \right\} + (E - 1)$$
(57)

Combining Equations 52, 53, and 55 gives

$$p = \exp \left[-\frac{(1+\delta)}{Z+Y-\delta}\right] \tag{58}$$

The value of E was again obtained from Equation 24. The average cross section of uranium over the resonance region, Σ_0 , is given by Equation 43. The scattering "absorption" cross section of the moderator over the resonance region, Σ_1^m , is given by Equation 44. Using values from Tables 1 and 2

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and Equations 20, 24, 30, 43, 44, 46, 47, 56, 57, and 58 the resonance escape probability was determined for Method B. These values of p are listed in Table 3 for the lattice configurations considered. The dry values for p were obtained by eliminating the terms for water in all equations.

F. Buckling

The theoretical buckling was computed using Equations 1 and 2. The diffusion length for each lattice configuration was calculated by (5, p. 280)

$$L^{2} = \frac{D}{\Sigma_{R}} = L_{g}^{2}(1 - f)$$
 (59)

where L is the diffusion length in pure moderator. The value of f used in each case was the theoretically determined value listed in Table 3. The Fermi age, γ , of the thermal neutrons for the lattice configurations was assumed to be the same as γ for the moderator. Murray (1, p. 123) gives the value of γ as 36 μ cm². The value of κ for each configuration was determined from the values of ϵ , γ , ϵ , and p listed in Table 3 for each configuration.

The volume of a cubical critical reactor having the given lattice configuration is

$$V_{T} = \frac{161}{B_{g}} \tag{60}$$

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The square of the lattice diffusion length and the buckling for each of the lattice configurations considered are listed in Table 4. The volume and cube side length of a cubical critical reactor for each considered lattice configuration are also listed in Table 4.

IV. EXPERIMENTAL INVESTIGATION

A. Description of Equipment

A picture of the subcritical assembly with a 8.5 in.

lattice spacing is shown in figure 3. The physical dimensions of the graphite assembly were 60 in. x 60 in. x 79 in.

The actual graphite used in the construction of the assembly was originally 7 in. diameter solid graphite rods. These rods were squared off to a 6 in. x 6 in. cross section (3.5 in. radius on the corners) and stacked as shown in Figure 3.

The top five rows of the graphite rods in the assembly were 5 in. x 6 in., and the bottom nine rows were 6 in. x 6 in.

The density of the graphite was determined from a weight and dimension measurement of a mass of graphite. The graphite density was found to be 1.56 g/cm³.

The graphite assembly was covered on the top and four sides with a 10 mil sheet of cadmium sandwiched between a 0.375 in. thickness of plywood and 0.125 in. of masonite. The cadmium sheet gave an effective "black wall" for thermal neutrons. Adding a 0.25 in. total spacing allowance for the graphite rods a horizontal section between the "black walls" of the assembly was 60.5 in. x 60.5 in. in area. The assembly was mounted on a concrete base, and tanks of water were placed under the graphite structure to insure that adequate

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shielding was effected with the neutron source in place. Figure 3 shows the relative placement of these tanks.

The lattice spacing was varied by changing the arrangement of the uranium filled process tubes in the assembly.

The 6 in. lattice, Lattice I, was the configuration with all the lattice holes filled with process tubes. The 8.5 in. lattice, Lattice II, was the configuration as shown on Figure 3. By removing alternate rows of the process tubes from the 8.5 in. lattice, the 12 in. lattice, Lattice III, was realized.

Five plutonium-beryllium neutron sources contained in individual right cylindrical containers were placed under the center of the graphite assembly. Each of these sources emitted approximately 1.63 x 10⁶ neutrons per second; therefore the total source strength was approximately 8.15 x 10⁶ neutrons per second. A cruciform geometry was chosen for the placement of the five sources. One source was at each of the cruciform ends, and one was placed at the cruciform center. The total source was in this way effectively contained in a circle of about 3.5 in. in diameter.

The cylindrical uranium slugs were 1.080 in. in diameter and 8.40 in. in length. Assuming a 40 mil cladding and a 200 mil slug end cap of 25 aluminum, the actual uranium fuel size was a rod 1.00 in. in diameter and 8.00 in. in length. The density of the uranium was determined from the weights

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and dimensions of several random sample slugs. The density of natural uranium determined in this way was 19.0 g/cm3.

The smallest lattice spacing investigated, the 6 in.

lattice, required 117 sections of 6061-T6 (commercial designation 618) aluminum tubing. The tubing sections had an outer diameter of 1.375 in., a wall thickness of 35 mils, and a length of 62 in. The composition of 618 aluminum is 0.25% copper, 0.60% silicon, 1.00% magnesium, 0.25% chromium, and the remainder aluminum.

The spacing wire composition was 25 aluminum and had a 0.102 in. diameter. The wire was used to center the uranium slugs in the process tube. Seven uranium slugs were loaded in each tube with a helical wrapping of wire around the slugs for spacing in the tube. Approximately 10 feet of wire was used for each seven slugs.

Figure 4 shows a scale drawing of an actual unit cell of the subcritical assembly with a loaded process tube in place. Number seven rubber stoppers were used at both ends of the process tubing to contain the water coolant. The stoppers were also used for the dry configurations to help contain the uranium slugs during handling of the loaded process tubes. Allowing two process tube lengths of wire for each tube, the effective thickness of the process tube was calculated to be 40 mils. The effective thickness of the water annulus was then found to be 0.107 in.

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Indium foils were mounted on flat aluminum plates which in turn were placed on an aluminum holder. The holder was designed so that the depth of penetration of each foil into the slots in the assembly could be accurately determined. The indium foils were 1.5 in. x 1.0 in. x 0.003 in. and had an average weight of 0.59h3 grams. The average thickness of these foils was 6.1h mg/cm². Figure 5 shows the foil holder and foil placement during counting. The reometry of the foil with respect to the class wall counting tube was held constant by use of the counter shelf holder shown in Figure 5.

A model 181A scaler manufactured by Nuclear-Chicago and a glass wall Gieger tube were used to count the beta activity of the irradiated indium foils. A conventional stop watch was used for the timing of the counting period.

B. Procedure

The uranium filled process tubes were loaded into the graphite assembly in varying arrangements for the three geometric lattices investigated. The annulus between the slug and the tube wall was filled with water for the wet configurations.

The neutron flux distribution was determined by the indium foil activation method. By determining the activity of a

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foil after a long period of irradiation and making an allowance for decay during the process of counting, the saturation activity for a given indium foil was obtained.

$$A_{\infty} = A_{t} e^{\lambda t} \tag{61}$$

where A, is the saturation activity,

A+ is the activity at time t,

λ is the decay constant for indium,

and t is the time after removal from the neutron flux.

The saturation activity is proportional to the neutron flux at an equilibrium state. The irradiation time of the indium foils for each run was in all cases at least 6.5 hours. This length of time corresponds to more than seven half-lives of indium as the half life for indium is 54 minutes. The indium foils used were not exactly all the same size and weight, and therefore a normalizing correction was made. Dividing the saturation activity for a given foil by its weight resulted in a normalized saturation activity. Since a constant geometry was maintained in the counter, this operation put all of the individual foil activities on the same basis. This normalized saturation activity is the activity which is tabulated in the Appendix, Table 5 through Table 10, for all of the foil positions in each of the lattice configurations investigated.

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Upon removing a foil, a three minute minimum decay time was given to each foil before beginning the count. This period of time eliminated any short lived decay components in the activated indium. All of the counts taken of the indium foils were three minutes in duration. The decay time was taken as the difference between the time of the foil's removal from the neutron flux and the mid-time of the count duration.

The foil holder slot positions on the front face of the subcritical assembly are shown on Figure 6. The horizontal x direction spacing was given letter designations A through J. The vertical z direction spacing was numbered vertically 1 through 13. The actual distance in in. from the east face was the horizontal y direction distance designation. The unit of spacing was 6 in. in all cases with the sole exception of a vertical spacing change to 5 in. at the position where the lattice structure changed to a 5 in. x 6 in. area.

as glass wall Gieger tube operating at 950 volts was used for all of the foil activity determinations. Before and after each series of runs, an operational check on the tube and scaler was made with a sample of radioactive strontium. The background activity remained essentially constant at an average of 44 counts per minute during the series of counting runs. Dead time corrections were significant only on a few of the higher counts.

The surveys taken of the various lattice configurations were as follows:

Lattices I and II, wet and dry cases.

- a. Vertical at x = 27 in.; y = 18 in. and y = 30 in.
- b. Horizontal, x direction, at y = 18 in. and y = 30 in.; z = 30 in.
- c. Horizontal, y direction, at x = 27 in.; z = 30 in.

Lattice III, wet and dry cases.

a. Vertical at x = 27 in.; y = 30 in.

Lattice without uranium.

- a. Vertical and horizontal, x direction, at y = 30 in.
- b. Herizontal, y direction, at x = 27 in.;z = 30 in.

Figure 6 is a diagram showing the foil positions.

Glasstone (5, p. 284) shows that the flux variation in the vertical direction at distances not too near the top of a rectangular subcritical assembly shape is

$$\emptyset(z) = Ce^{-\frac{y}{2}z} \tag{62}$$

with

$$\gamma^2 = \left(\frac{\pi}{a}\right)^2 + \left(\frac{\pi}{b}\right)^2 - B_m^2 \qquad (63)$$

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The term B_m^2 is designated as the material buckling. The dimensions of a critical reactor can be obtained by setting $B_m^2 = B_g^2$, the geometric buckling. With the material buckling equal to the geometric buckling, B^2 is defined as the buckling. The base dimensions a and b include the extrapolation length. At large distances from the assumed source plane the harmonic corrections are assumed to be negligible.

As the neutron flux is proportional to the indium foil saturation activity, a linear plot of the logarithm of $\beta(z)$ versus the vertical position z yielded the quantity - γ which is the slope of this plot. The base dimensions were equal in the assembly used in this investigation. By adding an extrapolation length of 0.71 γ to each side of the effective neutron "black wall", the square base dimensions became 62 in. Equation 63 can now be rewritten as

$$B^2 = 2\left(\frac{\pi}{a}\right)^2 - \chi^2 = 795 \times 10^{-6} - \chi^2 \tag{64}$$

where the units of B2 are cm-2.

V. RESULTS

The saturation activities for given feil positions of the configurations considered are tabulated in Tables 6 through 10 of the Appendix. Plots of these values, figure 7 through Figure 16, show the vertical and horizontal distribution of the neutron flux in the subcritical assembly for the lattice configurations investigated.

The theoretical and the experimental values of the buckling and critical reactor size for the various lattice configurations considered are listed in Table 4. Figure 17 shows the relationship between the theoretical and experimental buckling values for the wet and dry cases and the lattice spacing.

The y = 30 in. position of the vertical flux survey plots was used for the experimental determination of buckling. The vertical flux distribution in the z direction for the y = 18 in. position, Figure 7 and Figure 9, was plotted only to show that the flux variation at this position was also exponential in nature. Due to the critical nature of the slope of these vertical flux plots with respect to the buckling value, the buckling from the y = 18 in. position was not calculated. The buckling, Equation 64, is a function of the square of the slope, - %. Therefore a very small change in the quantity reflects a much larger change in the value of buckling.

A deviation from a true exponential nature was noted in the vertical flux plots at the lower and higher end positions of all surveys in the z direction. The lower end deviation was due to excess fast neutrons, 5 to 12 Mev, from the plutonium-beryllium neutron source. All of the neutrons from the source in this lower portion of the assembly had not as yet been moderated. The neutron absorption reaction in indium is for neutrons below 1.5 electron volts. The higher end deviation occurred approximately at the 59 in. height. This is the point where the lattice spacing changes for the three different geometrie lattices considered due to the construction of the assembly. The slope of the flux plots increased near this general position in all of the vertical survey plots. Statistical error in counting the small amount of activity at high z positions accounted for the relative increase in the dispersion of the counts at these positions. These effects can be observed on the plots shown on Figure 7 through Figure 11.

The vertical flux for the wet configuration was greater than the vertical flux for the dry configuration up to z = 36 in. for Lattice I, Figure 7, at the y = 18 in. position. A similar situation existed for Lattice I, Figure 8, at the y = 30 in. position with the cross ever at z = 50 in.

Figure 9 shows that the wet-dry cross over point of the flux plot for Lattice II at y = 18 in. occurred at z = 30 in. Similarly again, the wet-dry cross over point of the vertical

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flux distribution plot at y = 30 in. for Lattice II, Figure 10. and Lattice III. Figure 11. occurred at z = 42 in. and z = 38 in. respectively. The effect of the moderation of the water was greater than the effect of the water absorption for approximately the lower half of the subcritical assembly in all lattices investigated. The water moderation effect increased the thermal neutron flux by slowing up the fast neutrons. In the lower portions of the assembly, these fast neutrons are primarily from the source. This moderation effect by the water in the process tubes was more pronounced at the y = 30 in. position than at the y = 18 in. position due to the base center position of the source. Over the center, y = 30 in., the neutron flux consisted of more fast neutrons at a given low horizontal plane than other positions further off center. This excess of fast neutrons was moderated in part by the water. At the y = 18 in. position a water moderation effect was also experienced by the fast neutrons, but the greater graphite moderation due to the greater distance from the source caused the number of fast neutrons to be smaller than at the center positions. The number of fast neutrons due to fission was also larger at the center positions than at the outer positions of the assembly. This is due to the sine distribution of the thornal neutron flux in a horizontal plane in the assembly. Thermal neutrons caused the fissions in the natural uranium which produced fast newtrons and other fission products. The position of the maximum

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thermal neutron flux was therefore also the position of the maximum fast neutron flux due to fission.

The vertical flux survey for the case of the graphite lattice without uranium is shown on Figure 12. The dry configuration flux values for Lattices I, II, and III were cross plotted to indicate the cross over point on the flux plot without uranium. The flux plot of Lattice III crossed the no uranium lattice plot at a slightly higher point than the flux plot of Lattice II did. The flux of Lattice I had the lowest cross over point of the three lattices. The increase of neutron flux due to subcritical multiplication in Lattice I appeared to be less than the absorption effect of the uranium. This effect was not nearly so prenounced in Lattices II and III. The neutron flux plot for the no uranium lattice appeared to be truly exponential in character for all but the low and high extreme positions in the assembly.

The slopes of the vertical flux plots for the x = 27 in. and y = 30 in. position were determined, and it was found that the magnitude of these slopes varied as follows: the flux plot in Lattice II had the smallest slope and the flux plot in Lattice III had the greatest slope. The slope of the flux plot in Lattice I was slightly greater than the Lattice III slope. The greater the slope of the flux plot, the smaller the value of the buckling becomes. This slope variation was true for both the wet and dry configurations and was directly reflected in the buckling values calculated.

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There was little difference in the effect of subcritical multiplication between the dry cases of Lattice II and III.

From a vertical height of 45 in. and upwards, the flux in dry Lattice II was slightly higher than in dry Lattice III.

The absorption difference in these two lattices was apparently small.

The horizontal surveys for symmetry in the x direction for z = 30 in. are plotted in Figure 13 through Figure 15.

An extrapolation length was added to each end beyond the effective neutron "black wall". All of the symmetry plots were plotted as sine curves.

The horizontal x direction Lattice I flux, Figure 13, for the wet case was greater than the flux for the dry case at both y = 18 in. and y = 30 in. positions. The horizontal x direction Lattice II flux, Figure 13, showed that there was very little difference between the wet and the dry cases for either the y = 18 in. or y = 30 in. positions. The y = 30 in. position flux for both lattices was greater in magnitude than the y = 18 in. position flux due to the sine distribution in the y direction.

The effect of the water moderation appeared to be greater than the water absorption effect in Lattice I at both the y = 18 in. and y = 30 in. positions for the x direction survey. In the x direction survey for Lattice II, these effects were approximately equal for both y positions.

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Lattice II flux in the x direction at z = 30 in. had in all cases almost an ideal sine distribution. The flux in wet Lattice I had some random scatter over the center section of the herizontal survey. This variation perhaps was due to water moderation having a greater effect than the water absorption over the near center section. This net effect was more pronounced directly over the source.

Figure 14 shows a horizontal x direction comparison at z = 30 in. of the wet, dry, and without uranium configurations. Lattice I values of flux for both the wet and dry cases were below the flux values in the no uranium Lattice. The flux in wet Lattice I was again higher than the flux in dry Lattice I. In Lattice I, the absorption effect at the z = 30 in. position was obviously greater than the subcritical multiplication effect. Lattice II values of flux for the wet and dry cases are just slightly below the no uranium case. In this lattice the subcritical multiplication effect and the absorption effects were approximately equal.

A lattice comparison for the horizontal x direction at z = 30 in. is shown on Figure 15. The Lattice II flux was greater than the Lattice I flux in both the wet and dry configurations.

Symmetry (sine distribution) was shown in the y direction on Figure 16 for Lattices I and II at the x=27 in. and z=30 in. position. The plot shows that there was little difference between the wet and dry cases of either Lattice I

a sine distribution at the center positions of the wet configuration. Also the sine curve plotted for symmetry was slightly to the left of the points plotted on Figure 16.

This was probably due to the placement of the foil holders or some spreading of the graphite blocks from a Lattice I loading. The flux plots of the wet and dry configurations in the y direction for Lattice II are approximately the same as the flux plot of the no uranium lattice. There is again some dispersion at the center position in this comparison.

The results of the experimental and theoretical bucklings determined for all configurations considered are shown on Figure 17. The two theoretical methods used to determine the buckling for the dry configurations showed reasonable agreement, but the wet case theory was in disagreement. The results from Method A were high in comparison with the results from Method B for wet Lattices I, II and III.

The experimental buckling values for the wet configurations were lower than the experimental buckling values for
the dry configurations in all three lattice spacings investigated. The theoretical values of buckling determined for the
dry configurations, Methods A and B, were a little higher
than the experimental values of buckling for the dry configurations. The theoretical values of buckling obtained from
Method A for the wet configurations were high in comparison
with the experimental buckling values. The theoretical Method

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B gave buckling values for the wet configurations which were in excellent agreement with the experimental buckling values for the wet lattices.

For the natural wranium graphite assembly a maximum did occur for the wet and dry cases of the buckling versus lattice spacing curve, Pigure 17. This maximum occurred in both the experimental and theoretical analyses. The C/V atom ratios were 73 for Lattice I, 116 for Lattice II, and 292 for Lattice III. Davenport (8, p. 315) concluded that the maximum buckling for a given natural uranium fuel assembly should occur at a value of C/V between 50 and 100. The maximum buckling in this investigation of three lattice spacings occurred at about a C/V value of 146 for both the wet and dry configurations.

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VI. DISCUSSION OF RESULTS

The theoretical methods employed had the following probable errors. Accurate detailed neutron scattering and capture cross section data are not available in the literature for all materials. Corrections for varying densities and purities of the materials were not computed. A calculated disadvantage factor for uranium was used instead of a measured value. Values from the literature were used for the Fermi age and the various lattice diffusion lengths where experimental values again would have given more accurate results for the calculated buckling. There were cracks between the graphite blocks with a process tube uranium load in the assembly. These air spaces and the air effect around the process tube itself were assumed to be negligible. The effect of temperature and humidity on the results was also assumed to be negligible. Finally, one group neutron theory was used throughout the analysis.

The following comments can be made concerning the experimental methods employed. The harmonic corrections to the flux distributions obtained were assumed to be negligible. The positioning of the foils and the normalizing of the foil activity were subject to human error. Finally, and most important, the slope of the $\ln \phi(z)$ versus z direction curve must be determined with great accuracy. This slope value is very critical in determining the actual buckling. Repeat runs for

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consistancy at a given position should be taken from which an average value of activities at a position could be used for plotting and the buckling calculation. Varying the foil weight at a given position during the runs would tend to cancel out any nermalizing error.

The feasibility of an actual reactor with the process tubing, natural uranium, slug geometry, and water coolant used in this investigation was determined. Assuming 1250 channels, a water coolant, and 0.405 in. 2 flow area per channel the mass flow is 1.68 x 10⁶ lb /hr. Assuming a temperature difference of 70°F and using C_p = 1.06 for water at 400°F, the heat rate transfer is 366 megawatts. This heat rate transfer is large enough for a potential power reactor. The above assumptions are conservative in comparison with the experimental critical reactor volume determined for the wet 8.5 in. lattice configuration.

The process tubing did spread the graphite blocks a small amount due to the fact that some of the holes were smaller than the normal average designed size. A power drill of an appropriate size could enlarge these holes so that the process tubing would slide in and out of the assembly with ease and no spread would occur. It was found that a lattice change was more easily accomplished using the process tube uranium containment than with just the loose slugs. One end of the process tube was beveled to facilitate loading of the wire wrapped slugs. It is suggested that a number seven rubber stopper be

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well seated in the beveled end and a larger stopper be used at the other end. Coolant leakage would in this way be eliminated.

The E-3 position foil holder hole was a through hole in the y direction. This through hole would be of more use if it were moved up to the E-8 or E-9 positions. The E-3 position was too close to the source for a good symmetry flux survey.

The 8.5 in. lattice is the optimum lattice spacing which is possible with the subcritical assembly used. Suggested ideas for future study are the investigation of other coolants and a more detailed analysis of the 8.5 in. lattice for both the wet and dry configurations. Also, the effect of the reflection by the water contained below the source may be investigated to give a maximum source flux with the available sources in place. With the use of an additional inner process tube the effect of a variable water annulus could also be investigated.

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VII. CO CLUSIO 8

The moderation effect of the water was greater than the absorption effect of the water for approximately the lower half of the subcritical assembly for the three lattice spacings investigated. The thermal neutron flux in the lower portion of the assembly was greater in the wet configurations than in the dry configurations, and the reverse situation existed in the upper portion of the assembly. The 6 in. wet lattice had the lowest overall flux because the absorption effect of the greater amount of water and uranium was larger than the subcritical multiplication effect in this lattice.

The 12 in. lattice was "over moderated" with an apparent small subcritical multiplication effect. The optimum lattice investigated was the 8.5 in. lattice. In this lattice the water had very little effect on the flux distribution due to the balance of the water moderation and absorption effects.

The symmetry surveys showed that in the x and y directions that the flux did follow a sine distribution for both the wet and dry configurations.

The two theoretical methods used to determine the buckling for the dry configurations gave results with reasonable agreement. These theoretical bucklings for the dry cases were high in comparison with the experimental bucklings determined for the dry cases except for the 12 in. lattice. The two theoretical methods used to determine the buckling for the

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wet configurations gave results which were in disagreement. The method of Murray gave values of the buckling for the wet configuration of the 6 in. and 8.5 in.lattices which were very high in comparison with the experimental buckling values. The method of Rumsey and Volkoff gave values of the buckling for the wet configuration of the 6 in. and 8.5 in. lattices which were in excellent agreement with the experimental buckling values determined. The experimental buckling value determined for the 12 in. wet lattice was between the two theoretical buckling values determined for this lattice. The experimental buckling values for the dry cases were higher than the values for the wet cases in all lattice spacings investigated. The only experimental positive value of buckling for the wet configurations was the buckling value for the 8.5 in. lattice.

A maximum in the buckling versus lattice spacing curve did occur for both the wet and dry configurations. This maximum in buckling was found in both the theoretical and the experimental values determined. These buckling curves for the wet and dry configurations did not cross; hence a "fail-safe" behavior upon the loss of water coolant could not be expected from these results.

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Table 1
Dimensions for a unit cell

	TO THE TAIL TO THE TOTAL OF STATE OF THE TAIL		
Lattice I (6 in.), II (8.5 in.), and III (12 in		
ru,	uranium rod radius	1.270	cm
tal,	thickness of aluminum slug can	0.102	cm
t _w ,	effective thickness of water annulu	s 0.273	cm
t _p ,	effective thickness of process tube	0.102	cm
tair,	effective thickness of air annulus	0.455	om
r ₁ ,	equivalent inner radius of graphite	2.20	cm
Fquivalent	cross section areas for one cell		
Uraniu		5.06	cm
Slug c	en	0.84	cm
Water	coolant	2.61	om
Process	s tube	1.06	cm
Air		5.65	cm
Graphi	te, Lattice I	217.0	om
Graphi	te, Lettice II	434.0	cm
Graphi	te, Lattice III	668.0	cm
Volume per	slug		
v _u ,	uranium	103.0	CM
Val,	slug can and cap	23.0	cm.
Vw,	water	55.7	cm
v _p ,	process tube	22.6	ear
Vgl,	graphite, Lattice I	1,625	cm
v _{g2} ,	graphite, Lattice II	9250	cm
v _{g3} ,	graphite, Lattice III	18,500	cm

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Table 1 (Continued)

Lattice II, r₂, equivalent outer radius of graphite 8.60 cm

Lattice III, r₂, equivalent outer radius of graphite 11.94 cm

Lattice III, r₂, equivalent outer radius of graphite 16.76 cm

Table 2

Lattice cell material constants

Symbol	Value	Source
Σ_a^{al}	0.01323 cm ⁻¹	(5) and Equation 25
\sum_{a}^{r}	0.01556 cm ⁻¹	(5), (11) and Equation 25
Σ_a^u	0.324 cm ⁻¹	(1) and Equation 25
Σ_a^u	0.399 cm ⁻¹	(1) and Equation 25
Σ_{0}	0.0967 cm ⁻¹	Equation 43
Σ&	0.00036 cm ⁻¹	(5)
Σã	0.375 cm ⁻¹	(1) and Equation 25
Σ_1^m	0.01057 cm ⁻¹	(1) and Equation 144
$\Sigma_{\mathbf{t}}^{\mathbb{S}}$	0.354 cm ⁻¹	(1) and Equation 49
Σ_{a}^{w}	0.017 cm ⁻¹	(5)
Hu	0.675 cm ⁻¹	Equation 26
d'g	0.01992 cm ⁻¹	(5) and Equation 27

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Table 2 (Continued)

Symbol	Value	Source
H _W	0.3472 cm ⁻¹	(5) and Equation 27
fre	0.4218 cm ⁻¹	Equation 46
4re	0.1059 cm ⁻¹	Equation 47
cos 0	0.0555	Equation 50
qw/qg	20	(3)
₽ ₽	0.158	(5)
Fermi age,	7 _g 364 cm ²	(1)
Lg ²	2520 cm ²	(1)
PE	1.56 g/cm ³	Measured value
Pu.	19.0 g/cm ³	Measured value
S/M	.0828 cm ² /gm	Calculated value, Equation 42

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Table 3
Theoretical nuclear lattice constants

Method A				
Lattice	I	II	III	
DRY				
£	0.926	0.870	0.767	
р	0.823	0.909	0.955	
准 oo **	1.023	1.062	0.984	
TAN				
٤	0.901	0.847	0.751	
p	0.823	0.909	0.955	
k _∞ *	0.996	1.035	0.963	
	<u>Metl</u>	nod B		
Lattice	I	II	III	
DRY				
f	0.920	0.863	0.759	
p	0.836	0.915	0.958	
k oo	1.034	1.061	0.976	
WET				
f	0.882	0.818	0.710	
p	0.832	0.911	0.954	
k o *	0.985	1.008	0.910	

^{*}Evaluated using $\epsilon = 1.927$ and $\eta = 1.308$.

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Table 4
Buckling and critical reactor size

Theoretical Method A				
Lattice	I	II	III	
DRY Value				
L ² om ²	1.86	328	587	
B _m ² em ⁻²	41 x 10 ⁻⁶	86 x 10 ⁻⁶	-17 x 10-6	
V _{rem} 3	611 x 10 ⁶	200 x 10 ⁶	-	
Cube side, ft.	27.7	19.2		
WIT Value				
L ² cm ²	250	386	627	
R _m ² cm ⁻²	-6.5 x 10 ⁻⁶	46 x 10 ⁻⁶	-37 x 10 ⁻⁶	
v _{rem} 3	-	520 x 10 ⁶	ste	
Cube side, ft.		26.4	4 6 9 8 6 9 9	
	Theoretic	al Method B		
Lattice	I	II	III	
DRY Value				
L ² cm ²	201	345	607	
B _m ² cm ⁻²	59 × 10 ⁻⁶	83 × 10 ⁻⁶	-25 x 10 ⁻⁶	
v _{rem} 3	357 x 10 ⁶	212 x 10 ⁶	-	
Cube side, ft.	23.2	19.6	-	
WET Value				
L ² cm ²	298	459	730	
B _m ² om ⁻²	-23 x 10 ⁻⁶	9.7 × 10 ⁻⁶	-85 x 10 ⁻⁶	
v _{rom} 3	-	5340 x 10 ⁶	-	
Cube side, ft.		57.4		

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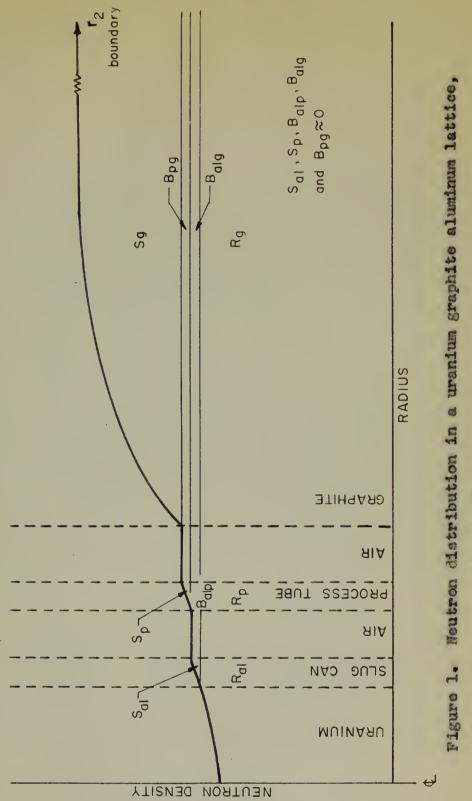
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Table 4 (Continued)

Experimental				
Lattice	I	II	ııı	
DRY Value				
B _m ² cm ⁻²	35 x 10 ⁻⁶	70 x 10 ⁻⁶	-5 x 10 ⁻⁶	
V _T om ³	778 x 10 ⁶	275 x 10 ⁶	40	
Cube side, ft.	30.1	21.3	+	
WFT Value				
B _m ² cm ⁻²	-23 x 10 ⁻⁶	12 × 10 ⁻⁶	-48 x 10 ⁻⁶	
V _T em ³	••	3880 x 10 ⁶	00	
Cube side, ft.	-	51.5	00	

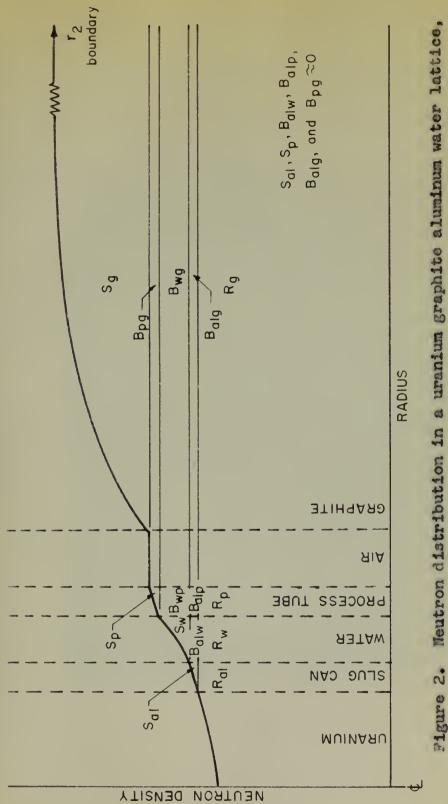
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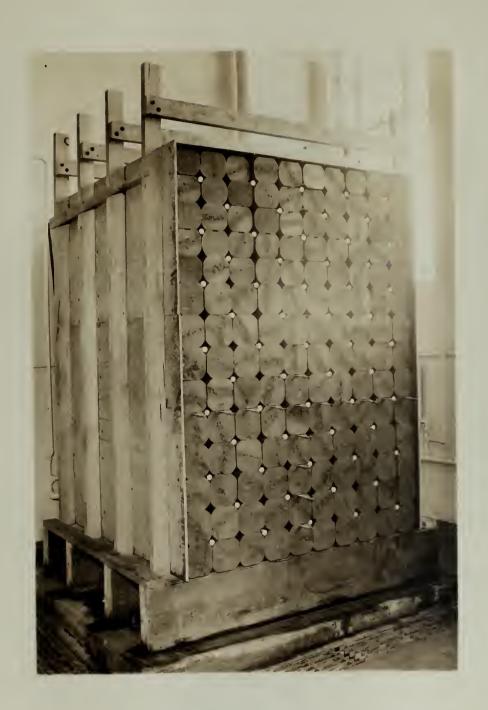


wet configuration. Figure 2.



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Figure 3. Subcritical assembly





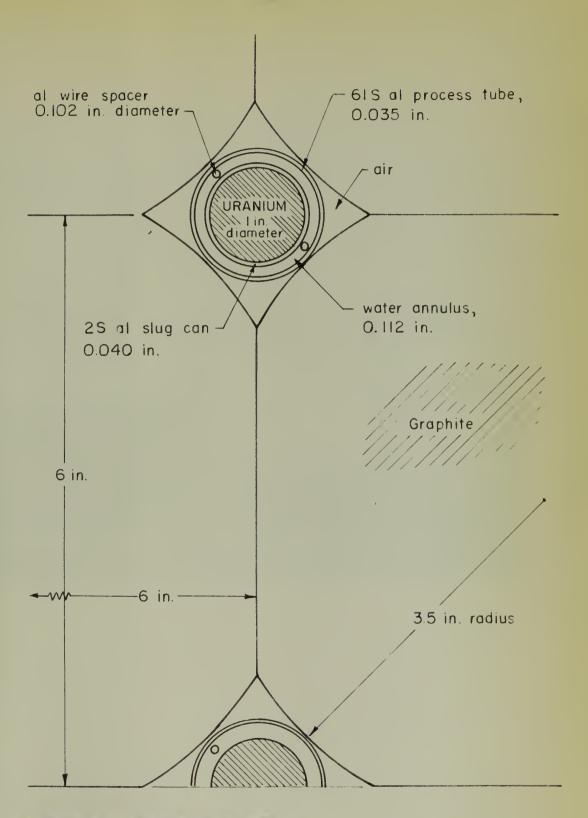
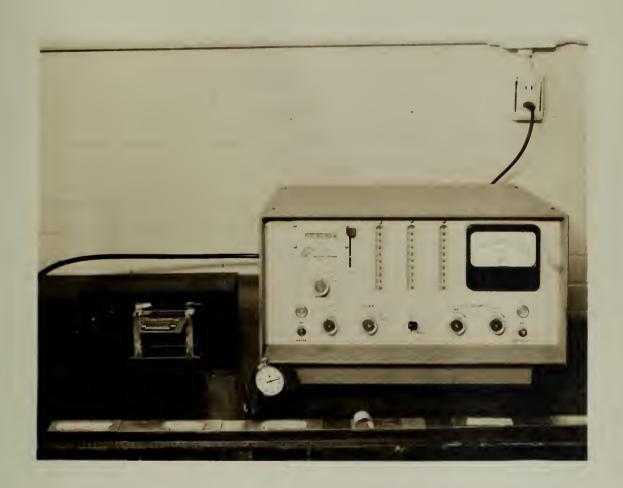


Figure 4. Actual unit cell.



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Figure 5. Counting equipment.





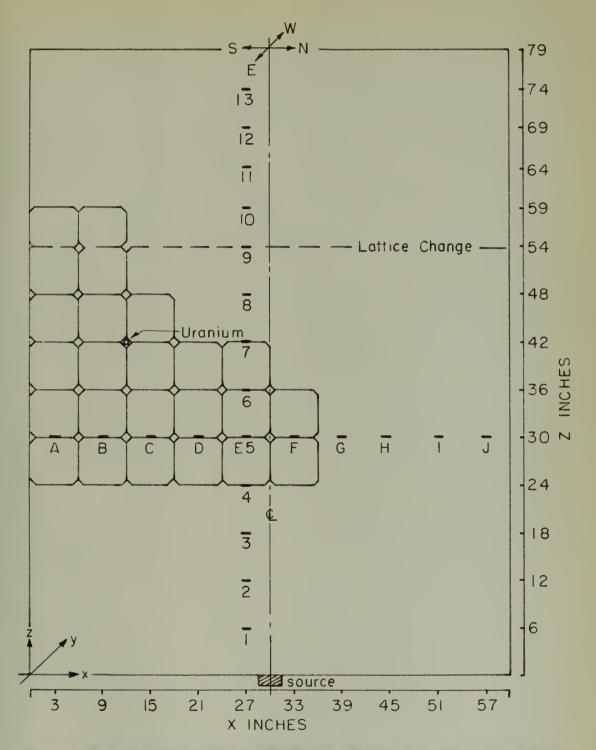


Figure 6. Front view of assembly showing foil positions.



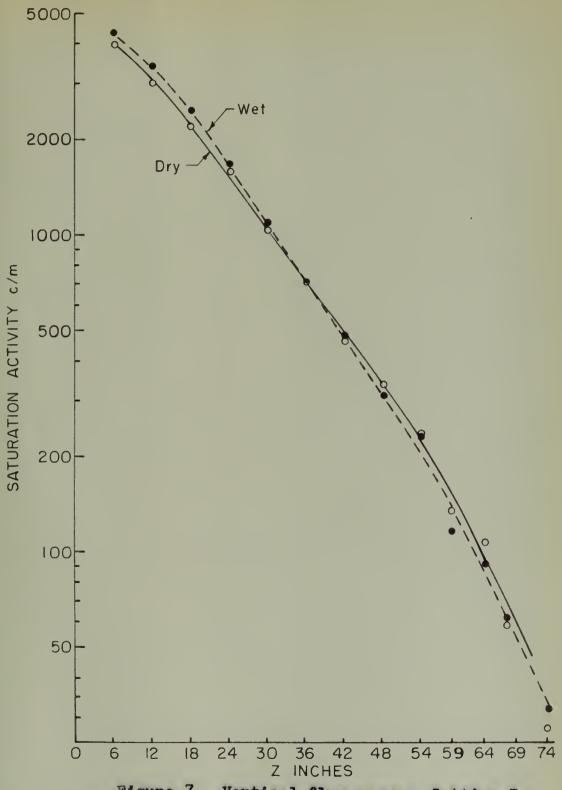


Figure 7. Vertical flux survey, Lattice I, x = 27 in., y = 18 in.



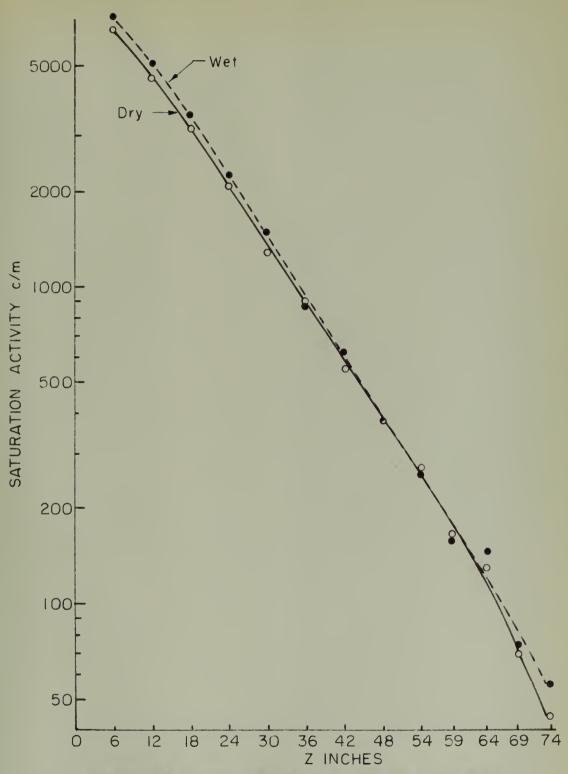


Figure 8. Vertical flux survey, Lattice I, x = 27 in., y = 30 in.



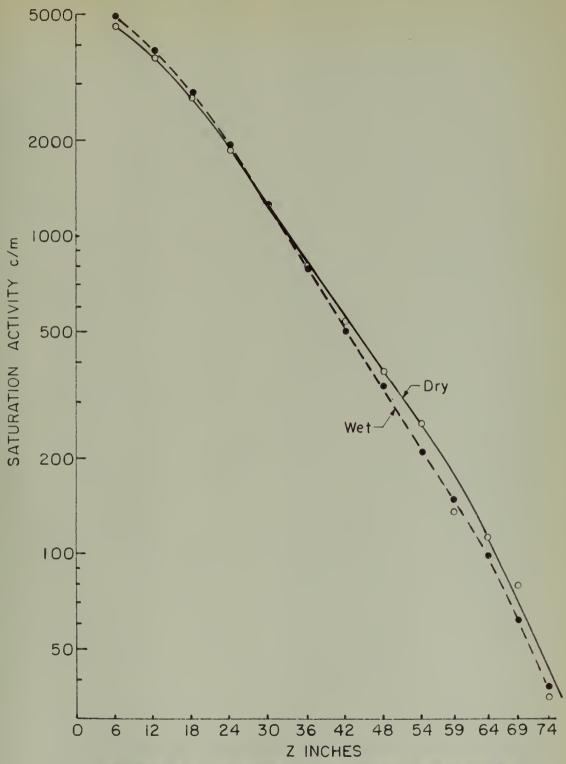


Figure 9. Vertical flux survey, Lattice II, x = 27 in., y = 18 in.



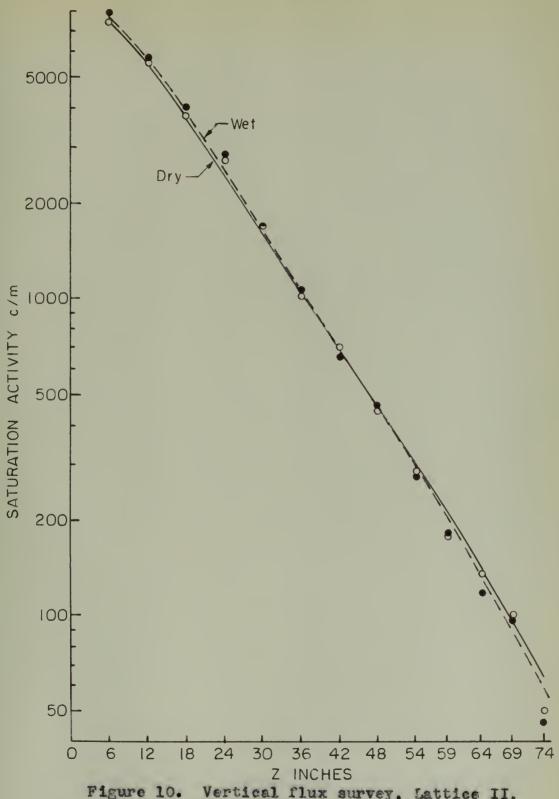


Figure 10. Vertical flux survey, Lattice II, x = 27 in., y = 30 in.



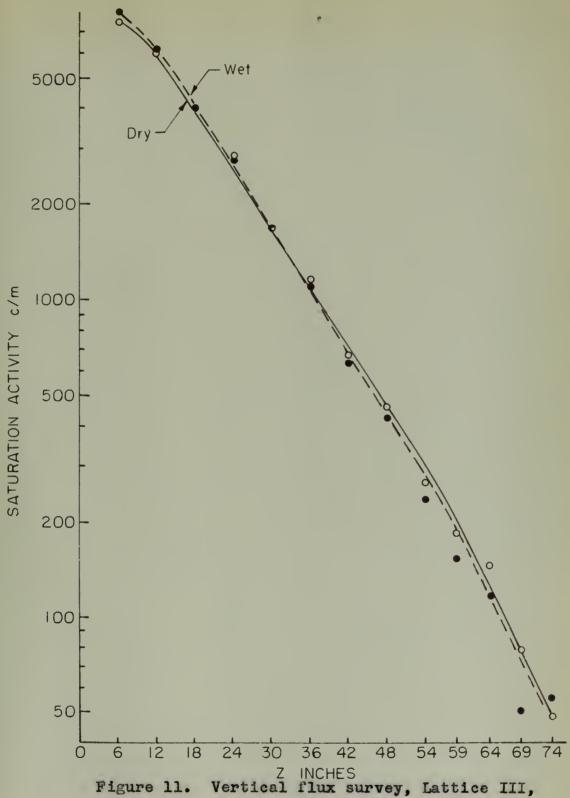


Figure 11. Vertical flux survey, Lattice III, x = 27 in., y = 30 in.



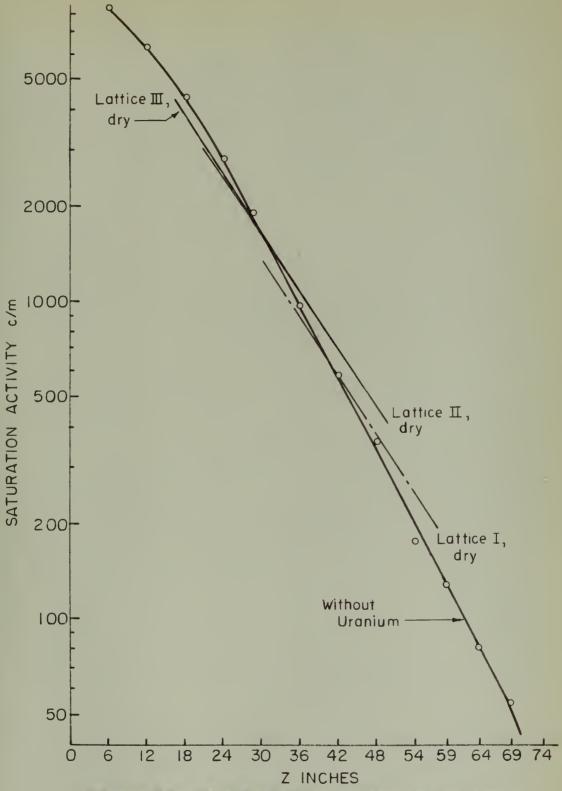


Figure 12. Vertical flux survey comparison, x = 27 in., y = 30 in.



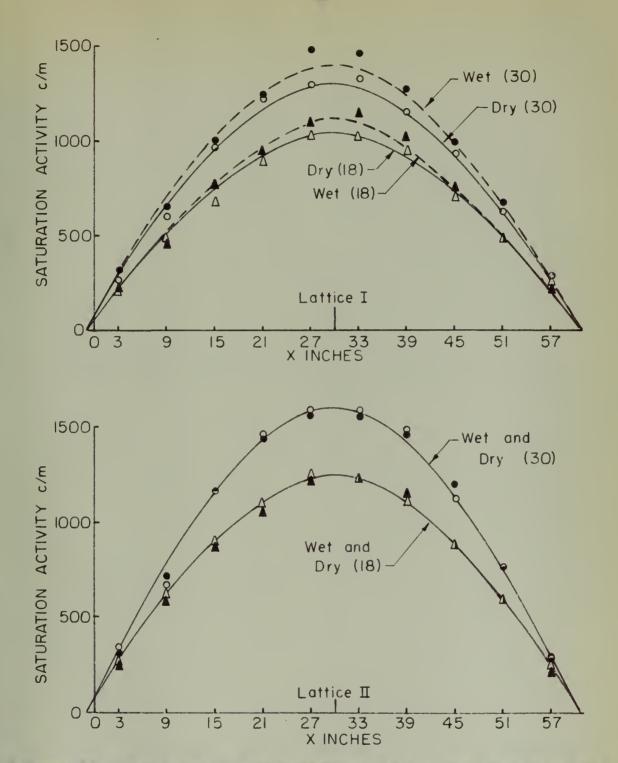


Figure 13. Horizontal flux survey, x direction, Lattice I and II, z = 30 in., y = 18 in. and y = 30 in.



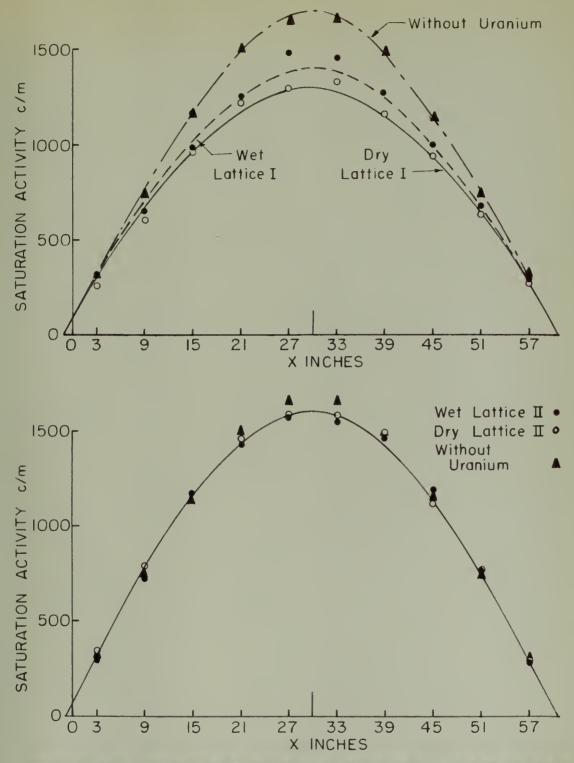
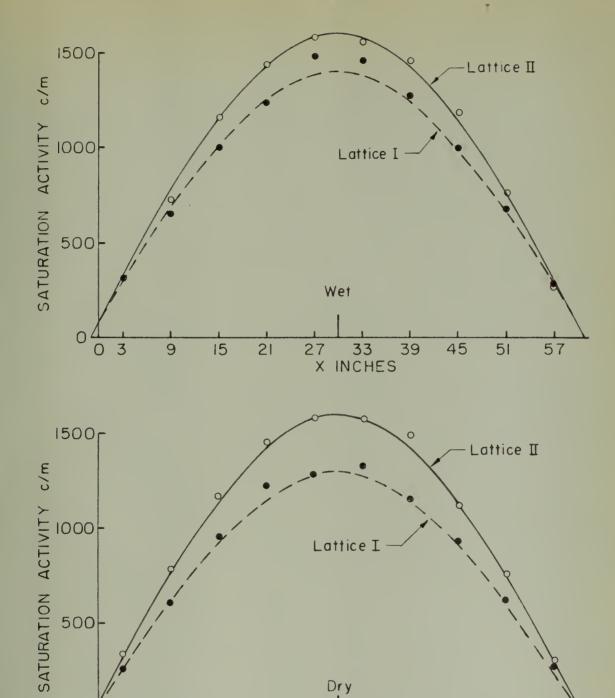


Figure 14. Horizontal survey, x direction, configuration comparison, y = z = 30 in.





Pigure 15. Horizontal survey, x direction, Lattice comparison, y = z = 30 in.

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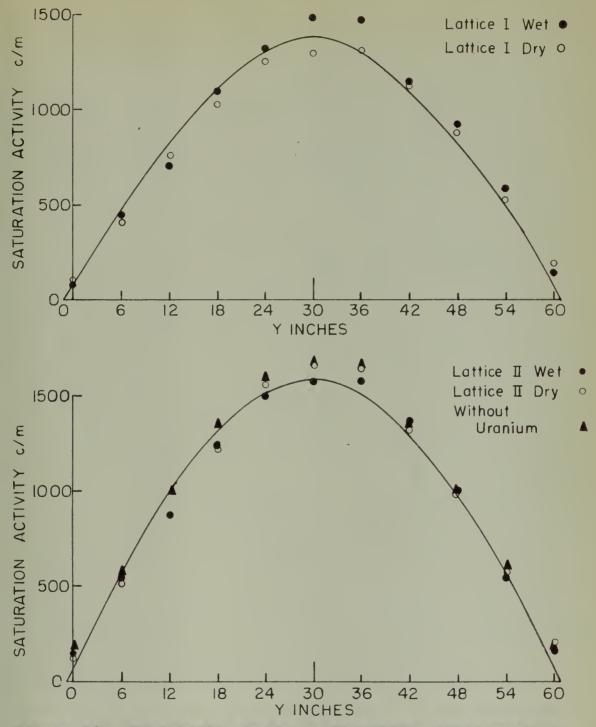


Figure 16. Horizontal survey, y direction, configuration comparison, x = 27 in., z = 30 in.



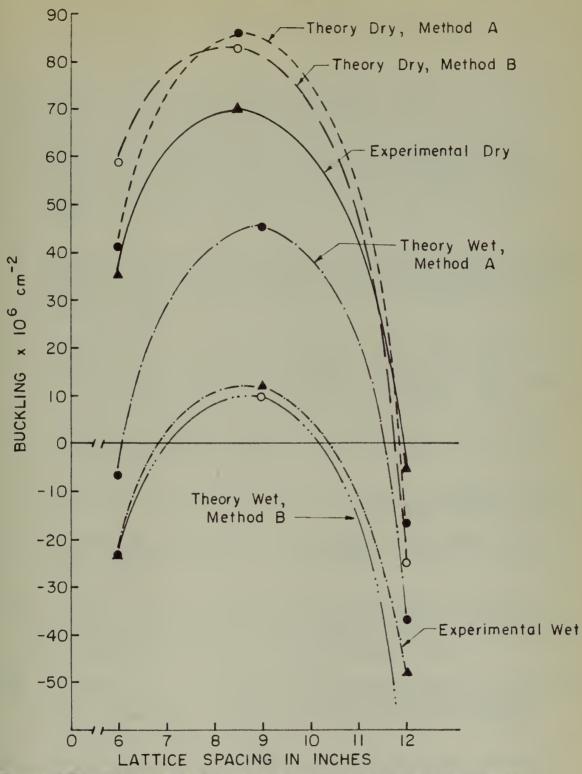
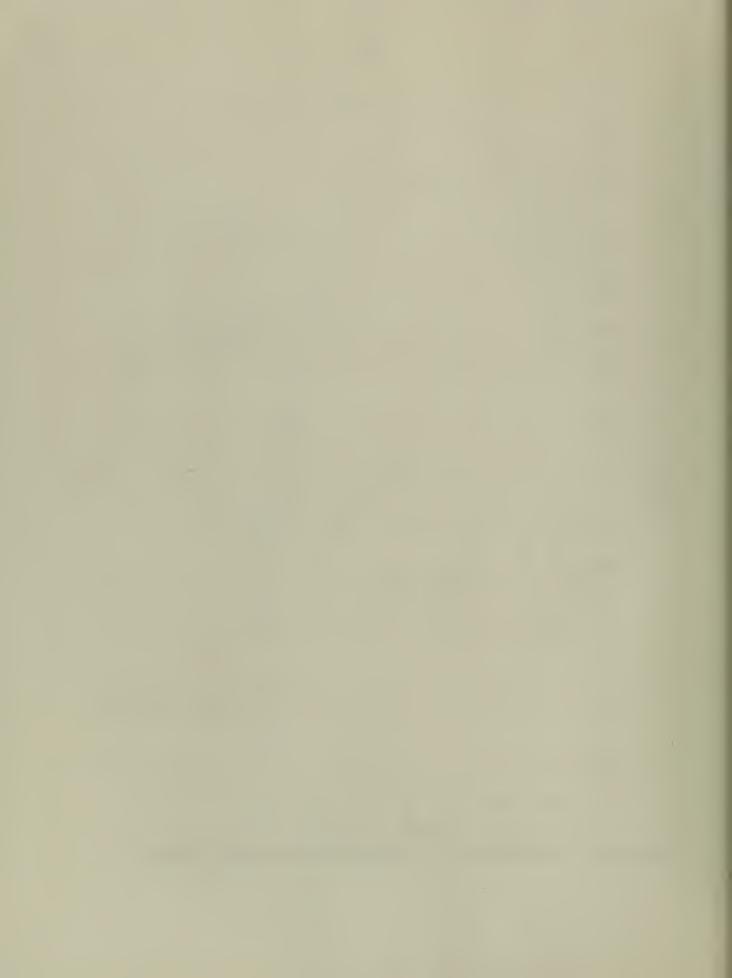


Figure 17. Theoretical and experimental buckling curves.



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IX. ACKNOWLEDGEMENTS

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X. APPENDIX



Table 5

Vertical flux survey Lattice I

	Saturation Activity			Saturation Activity	
Position	DRY	WET	Position	DILY	WET
E1-18	3903	4350	E130	6508	7180
E2-18	3040	3395	E2-30	14580	5110
E3-18	2192	21,60	E3-30	3170	3493
E4-18	1580	1681	F4-30	2085	2250
E5-18	1029	1095	E5-30	1290	1482
E6-18	716	707	E6-30	888	870
E7-18	465	1478	E7-30	552	620
B8-18	335	313	E8-30	376	378
E9-18	238	230	E9-30	268	253
N10-18	135	115	E10-30	163	158
E11-18	107	91	F11-30	129	146
E12-18	59	62	E12-30	69	74
E13-18	28	32	E13-30	717+	56

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Table 6

Horizontal flux survey Lattice I

	Saturation Activity C/N			Saturation Activity	
Position	DAY		Position	DNY	WET
A5-18	203	226	A5-30	256	321
B5-18	489	469	B5-30	605	650
c5-18	678	765	c5 - 30	958	990
D5-18	893	950	D5-30	1223	1237
E5-18	1029	1095	E5-30	1290	1482
25-18	1030	1145	F5-30	1330	1453
05-18	952	1020	05-30	1163	1270
H5-18	705	7148	H5-30	939	994
15-18	505	504	15-30	629	671
J5 -1 8	214	223	J 5-30	272	282
E5-0	115	73	E5-36	1306	1465
¥5-6	412	142	15-42	1131	1131
E5-12	759	709	E5-48	875	914
F5-18	1029	1095	ES-54	525	583
E5-24	1247	1320	E5-60	180	150

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Table 7
Vertical flux survey Lattice II

	Saturation Activity			Saturation Activity	
Position	DRY	WET	Positio:	DRY	WET
E1-18	4590	4900	E1-30	7400	7815
E2-18	3665	3802	E2-30	5505	5690
E3-18	2720	2790	E3-30	3768	3975
E4-18	1899	1930	E4-30	2680	2607
E5-18	1241	1235	E5-30	1583	1571
E6-18	801	784	E6-30	1009	101,9
E7-18	536	499	77-30	707	651
E8-18	376	332	E8-30	14110	453
E9-18	255	208	E9-30	282	278
E10-18	135	147	E10-30	175	180
E11-18	111	98	E11-30	135	118
E12-18	79	61	E12-30	100	96
E13-18	35	38	E13-30	50	46

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Table 8

Horizontal flux survey Lattice II

Position	Saturation Activity			Saturation Activity	
	DRY	WIT	Position	DRY	WET
A5-18	262	252	A5-30	340	304
B5-18	632	607	B5-30	791	728
c5-18	898	926	C5-30	1170	1169
D5-18	1105	1055	P5-30	1456	1435
E5-18	1241	1235	E5-30	1583	1571
V5-18	1230	1227	P5-30	1578	1550
65-18	1111	1156	65-30	1487	1 460
H5-18	891	886	H5-30	1120	1189
15-18	602	595	15-30	762	759
J5-18	266	221	JS-30	308	291
E5-0	117	148	E5-36	1641	1572
E5-6	511	541	E5-42	1347	1360
15-12	887	874	E5-48	965	1002
E5-18	1241	1235	E5-54	576	535
E5-21	1550	1499	E5-60	195	160

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Table 9

Vertical flux survey Lattice III

		n Activity	
Position	DRY	WET	
E1-30	7500	7985	
E2-30	5945	6150	
E3-30	3960	3990	
E4-30	2813	2742	
E5-30	1660	1658	
E6-30	1152	1093	
E7-30	669	637	
E8-30	1458	425	
E9-30	265	234	
E10-30	184	153	
E11-30	148	118	
E12-30	79	51	
E13-30	49	56	

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Table 10
Lattice flux survey without uranium

Position	Saturation Activity C/M	Position	Saturation Activity
E1-30	8365	E5-0	172
T.2-30	6290	E5-6	568
E3-30	14408	B5-12	992
E4-30	2795	E5-18	1339
E5-30	1655	E5-24	1590
F6-30	965	£5-36	1639
E7-30	587	E5-42	1320
E8-30	361	E5-48	990
E9-30	176	E5-54	615
E10-30	128	E5-60	183
E11-30	81		
E12-30	214		
113-30	22		
A5-30	320	G5-30	1486
B5-30	736	H5-30	1143
05-30	1161	15-30	735
D5-30	1500	J5-30	318
F5-30	1669		

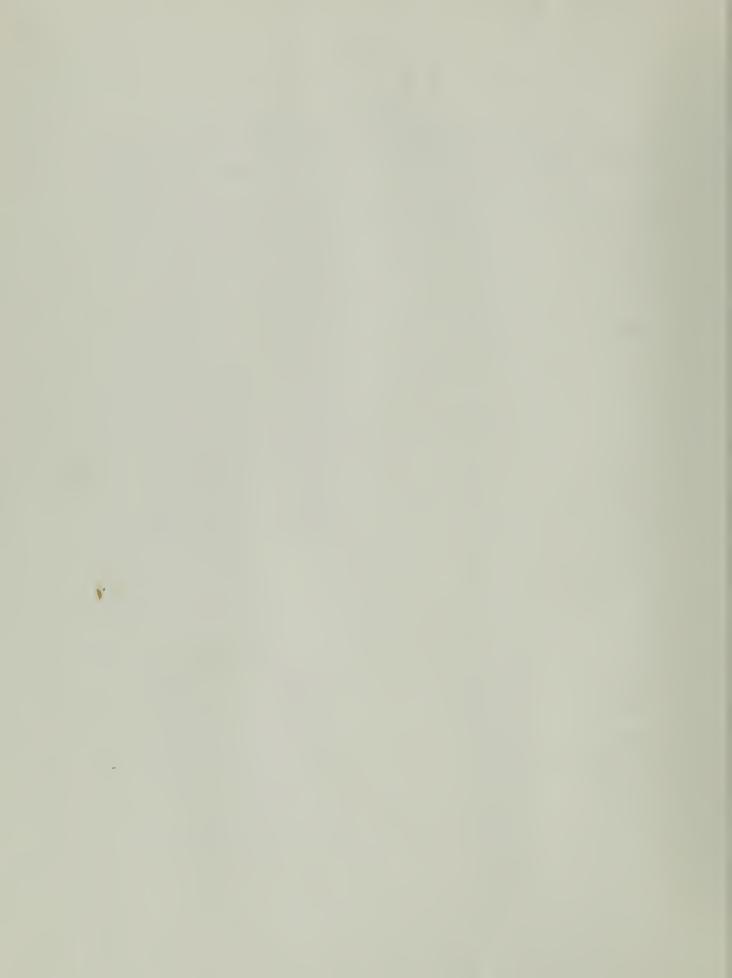
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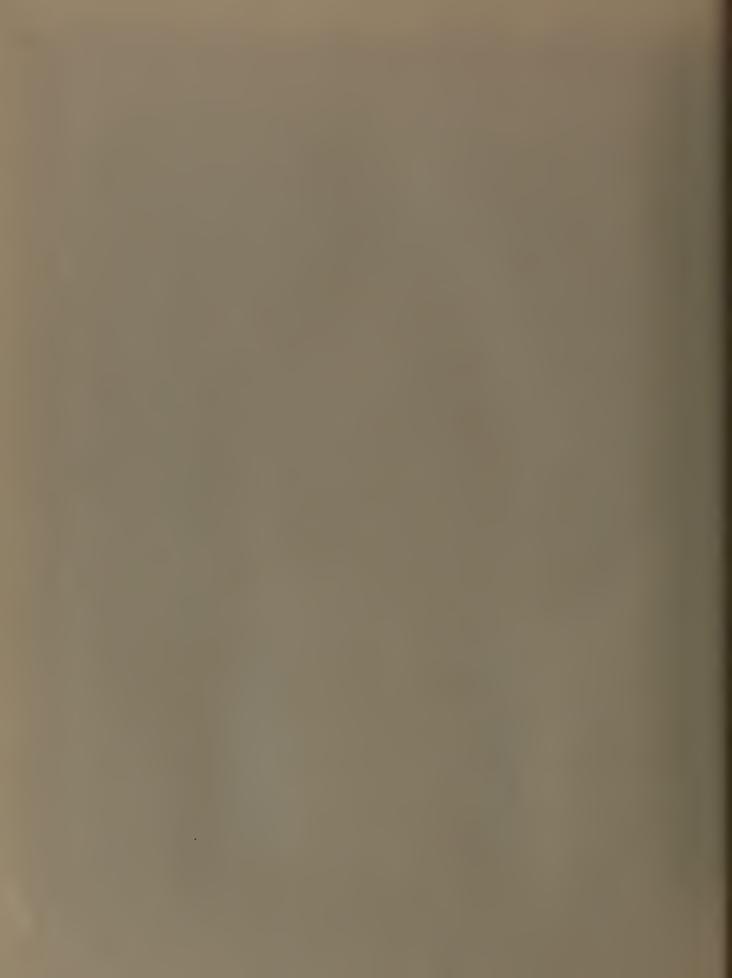












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